Open Access

Proposing an Approximate Mathematical Model to Conduct the Calculations of Radioactive Cs¹³⁷ in the Plant

Ghassan E. Arif^{*} Alaa A. Awad^{**}

Mohammed A. Hilal***



* College of Education for Pure Sciences, Tikrit University. ** College of Education for Pure Sciences, Anbar University. ***Middle Technical University.

ARTICLE INFO

Received: 07 / 5 /2017 Accepted: 05 / 06 /2017 Available online: 00/04/2017 DOI: 10.37652/juaps.2017.141532 **Keywords:** Mathematical Modeling, The Radioactive Cesium Cs¹³⁷, Mathematical Model, Physical Problem, Nevill's Method.

ABSTRACT

This study aims at calculating theoretically the radioactive of cesium Cs¹³⁷ in the plant of Nineveh governorate by selecting 50 positions as samples of the study. The calculations are carried out by constructing a mathematical model that determines theoretically the radioactive of cesium Cs¹³⁷ in the plant. In this paper, the main features and process of mathematical modeling is stated and used clearly in the process of constructing the mathematical model which conducts the determination of the radioactive of cesium Cs¹³⁷. The values calculated by the proposed mathematical model show that Cs¹³⁷ radioactive range is: (1.0832 in (A₄₂ & A₄₂) – 4.1020 in (A₄₈)) Bq/kg in plant. These calculations are conducted by comparing the results, obtained from the constructed model, with the values of other references. The result of this comparison shows good agreement with other literatures.

1- Introduction

In the recent years; the process of the mathematical modelling has become an essential tool in understanding and solving many physical problems, i.e. mathematical modeling is a powerful tool for analyzing physical problems that allows one to develop and test hypotheses which can lead to a better understanding of the physical process. It is defined as the application of mathematics to address problems in real life, or problems in mathematics itself, or problems in other sciences by converting these problems into mathematical problem, and then treating and solving them. Then we should choose the best solutions that fit with the nature of the problem we are dealing with [1].

Hence, the modelling process is always evolving so as to gain a deep understanding of the mathematical aspects of the problem. Moreover, the mathematical modeling is one of the modern trends in the development of mathematics education and having a societal role in addressing some of the issues and problems of society; it is the trend towards the applications of mathematics in other sciences, and the training of students to recruit mathematics to solve real problem [2].

Mathematical modeling is defined as a dynamic process that is used to analyze mathematically the problem or the situation in the field of physics, chemistry, biology or any area of human knowledge. It is simply known as a process of building a mathematical model to solve certain physical problem. Mathematical model is a description of a

^{*} Corresponding author at: College of Education for Pure Sciences, Tikrit University .E-mail address:

system where the relationships between variables of the system are expressed in mathematical form. Variables can be measurable quantities such as size, length, weight, temperature, unemployment level, information flow, etc. Most laws of nature are mathematical models in this sense. For example, Ohm's law describes the relationship between current and voltage for a resistor; Newton's laws describe relationships between velocity, acceleration, mass, force, etc. [3]

Connecting mathematics to other sciences like physics, engineering, medicine, etc., by using the mathematical modeling can help reduce the gap between theory and practice, and also help solve many problems in life. One of these problems is finding the calculation of radioactivity for cesium Cs¹³⁷ in plant, which represents the main aim of this paper.

Cesium-137 is a valuable plant redistribution tracer for many environments [4]. Cs^{137} was present into the atmosphere as a result of nuclear weapon tests nuclear fission. Cesium-137 is a major radionuclide in spent nuclear fuel, high level radioactive wastes resulting from the processing of spent nuclear fuel, and radioactive wastes associated with the operation of nuclear reactors and fuel reprocessing plants. The main period of cesium from nuclear weapon was in the 1950s and 1960s with the maximum cesium deposition in 1963. Cs^{137} deposition depends on the latitude and amount of precipitation [4].

The aim of this study is thus to find the calculation of radioactive Cs^{137} concentrations in plant of Nineveh governorate through constructing a mathematical model. Mathematical model is a mathematical form like a formula or equation that reflects the important features of a given situation and is shown to fit within the general context of problem solving. The arts and crafts of mathematical modeling are exhibited in the construction of models that not

only are consistent in themselves and mirror the behavior of their prototype, but also serve some exterior purpose [5]. The purpose of the current proposed model is to assist the physicists to conduct theoretically their calculations. The study area is the Environment of Nineveh Governorate, which is a north-west part of Iraq, and its altitude is ranging 730 F(223 m) above sea level [6].

2. The Model Formulation

In this study, the method of formulating the model is introduced through discussion of the techniques that are used in building the model. The mathematical model, which is proposed in this study, can be formulated through different forms. These forms depend on N, where N refers to the net area under the peak of the Gama energy used for measurement in the spectrum. Generally speaking, the mathematical model is a mathematical representation that includes constants, variables and mathematical functions, and is in the form of mathematical equation, inequality variance, graph, or table [7]. The mathematical models are based on the use of input equations and the mathematical concepts in its structure, where the final outputs of a particular research process are determined in terms of the various inputs, processes and involved activities, to take a form of a mathematical equation [7].

The mathematical model of the present study consists of a specific number of variables and parameters, the definition of these variables, measurement of these variables, and composing a mathematical relationship between these variables. It is a deterministic one and based on theoretical determinations. Each of the variables in the mathematical formulation is selected carefully and considered to assess their significance to the physical problem in the study, suggesting hypotheses or conclusions that can be tested physically. Upon comparison with experimental results, the model can be modified to more accurately emulate the problem. This iterative process of calculating model results and making physical comparisons can continue to the point at which the model suggests appropriate solutions to the problem and make realistic predictions.

In constructing the mathematical model, the current study counts on several steps and guidelines. In the first step, it is necessary to understand the problem and identify the data required in building the model. Then, it is important to make the necessary assumptions for the construction of the mathematical model: here what is needed is to consider and think carefully to reflect on the data, besides, studying the interrelations between variables, i.e., hunching the between the relationship variables and then formulating it in a mathematical image such as equation, variance, graphic shape. The next step is constructing the model through combining the parts of the model to

get the mathematical model, modifying it several times to get the best image of the model [8]. The mathematical model constructed in the present study is derived from finding a relationship between variables and parameters in a form of a mathematical equation. This equation is built manually through several manual trails [9-11] and revisions till we get the final form of the equation as shown in the following

$R_c = 0.133 \lambda \sqrt[3]{0.77 N^2 - 1000} , \quad (1)$

where R_C is referring to radioactive, and N is referring to the net area under the highest light for Gama energy which is used in measuring the spectrum. λ is a parameter is appropriate for all R, $\lambda = 1$.

After formulating the mathematical equation that is needed in conducting the calculations, the

model is applied by using input data (N) to obtain the output data. Then we compared the output data with the experimental values of other references [12]. The result of comparison proves that the error percent is very low, where we get the less error percent in the area (A_{25}), which is 0.000 as shown in the following table.

Table 1. Comparison between the values of the Rc in plant, which are determined by the proposed approximation mathematical model, and the experimental values [12].

experimental values [12].										
No.	Area	Ν	Rc	Rc	%					
1.01	(A)	- 1	Exp. [12]	Det.	,,,					
1	A1	96	2.52	2.4296 1.5231	0.036					
1	A 1	70	2.32	2.2270	0.000					
2	A ₂	57	1.49	1.5231	0.022					
3	A3	86	2.26	2.2270	0.014					
4	A4	76	1.99	2.0092	0.009					
5	A5	59	1.55	1.5812	0.02					
6	A ₆	81	2.13	2.1203	0.004					
7	A 7	72	1.89	1.9164	0.013					
8	A 8	69	1.8	1.8442	0.024					
9	A9	80	2.1	2.0985	0.0009					
10	A10	99	2.6	2.4881	0.043					
11	A11	60	1.58	1.6094	0.018					
12	A12	80	2.1	2.0985	0.0009					
13	A ₁₃	78	2.05	2.0542	0.001					
14	A14	58	1.52	1.5524	0.021					
15	A15	84	2.21	2.1848	0.011					
16	A16	77	2.02	2.0318	0.005					
17	A17	68	1.79	1.8195	0.016					
18	A18	88	2.31	2.2686	0.018					
19	A19	79	2.07	2.0765	0.002					
20	A20	75	1.97	1.9863	0.008					
21	A21	66	1.73	1.7693	0.022					
22	A22	78	2.05	2.0542	0.001					
23	A ₂₃	87	2.28	2.2479	0.014					
24	A ₂₄	64	1.68	1.7176	0.022					
25	A25	81	2.12	2.1203	0.000					
26	A26	88	2.31	2.2686	0.018					
27	A27	52	1.36	1.3654	0.003					
28	A28	47	1.23	1.1814	0.039					
N	ote: (A) refe	Note: (A) refers to the samples of (28) area							

Note: (A) refers to the samples of (28) areas.

To clarify the relationship between the output values obtained from the constructed mathematical model and the experimental values [12], the figures are plotted to show a comparison between these obtained values and experimental one depending on the area (N) as shown in the following figures.

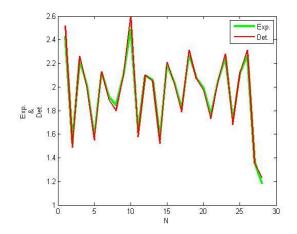


Fig.1 Compression between the values obtained via the proposed approximate mathematical model in table 1, and the experimental values [12].

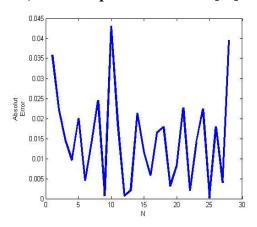


Fig.2 Errors between the values obtained by the proposed approximate mathematical model in table 1, and the experimental values [12].

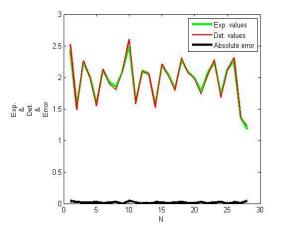


Fig.3 Comparison between proposed mathematical model and the experimental value [12], and errors

After building the model, it is necessary to solve the mathematical model by using Algebraic and analytical methods, differentiation, and graphic shapes. The current model is solved by the section method as shown in the following:

$$R_c = 0.133 \lambda \sqrt[3]{0.77 N^2 - 1000}$$

Define f(N) and g(N) are two functions of N.

$$f(N) = 0.133 \lambda \sqrt[3]{0.77 N^2 - 1000}$$

$$0 = 0.133 \lambda \sqrt[3]{0.77 N^2 - 1000}$$

$$0 = 0.77 N^2 -1000$$

$$1000 = 0.77 N^2$$

$$1000 = (0.77 N) N$$

$$N = \frac{1000}{0.77 N}$$

$$2N = \frac{1000}{0.77 N} + N$$

$$N = \frac{1}{2} \left(\frac{1000}{0.77 N} + N\right)$$

$$g(N) = \frac{1}{2} \left(\frac{1000}{0.77 N} + N\right)$$

$$g(N) = 0.1 < 1$$

$$g(N) = \frac{1}{2} \left(\frac{1000}{0.77 N} + N\right)$$

$$N_i = g(N_i - 1)$$

$$N_0 = 42$$

$$g(N_0) = N_1 = \frac{1}{2} \left(\frac{1000}{0.77 \Box 42} + 42\right) = 36.46$$

$$N_2 = g(N_1) = \frac{1}{2} \left(\frac{1000}{0.77 \Box 36.46} + 36.46\right) = 36.039$$

$$N_3 = g(N_2) = \frac{1}{2} \left(\frac{1000}{0.77 \Box 36.039} + 36.039\right) = 36.0374985391$$

$$N_4 = g(N_3) = 36.0374985078$$

$$\varepsilon = \left| \frac{N_4 - N_3}{N_3} \right| = 0.000000009$$

3- The relative and absolute errors:

One commonly distinguishes between the relative error and the absolute error.

Given some value of Rc and its $Rc_{approximation}$, the absolute error is

 $\varepsilon = \left| Rc_{approximation} - Rc \right|,$

where the vertical bars denote the absolute value. If

 $Rc \neq 0$, the relative error is

$$\eta = \frac{\varepsilon}{|Rc|} = \left|\frac{Rc_{approximation} - Rc}{Rc}\right| = \left|\frac{Rc_{approximation}}{Rc} - 1\right|$$

and the percent error is

$$\delta = \eta \times 100\% = \frac{\varepsilon}{|Rc|} = \left|\frac{Rc_{approximation} - Rc}{Rc}\right| \times 100\%$$

In words, the absolute error is the magnitude of the difference between the exact value of Rc and the Rc approximation. The relative error is the absolute error divided by the magnitude of the exact value of Rc. The percent error is the relative error expressed in terms of per 100 [13].

4- Mathematical Model Validity:

To test the validity of the proposed mathematical model, the data has been extended to include extra (20) positions as study samples. The calculations are conducted by using eq. (1).

$$R_c = 0.133 \lambda \sqrt[3]{0.77 N^2 - 1000}$$
, (1)

where R_C is referring to radioactive, and N is referring to the net area under the highest light for Gama energy which is used in measuring the spectrum. λ is a parameter is appropriate for (A₂₉ - A₃₆, λ =1.082), and (A \geq A₃₇, λ = 1.1467).

The resulted calculations for some of these positions (about eleven positions) have been compared to the experimental values of other references. It is found that there is a well conformity between the data readings obtained from the proposed mathematical model and the experimental values as shown in table2.

While the calculations of the other extended positions (9) are conducted approximately which proved the applicability of the model to calculate the radioactive theoretically. Conducting theoretical calculations are very important as they do not require physical laboratories or going to the positions themselves, so the process of calculating becomes easy to the physicists. This represents the aim of the current study.

No.	Area (A)	N	Rc Exp.[12]	Rc Det.	%
29	A29	42	1.1	1.0832	0.015
30	A30	42	1.1	1.0832	0.015
31	A ₃₁	45	1.18	1.1867	0.004
32	A32	105	2.75	2.8181	0.023
33	A33	106	2.78	2.8384	0.019
34	A ₃₄	109	2.86	2.8985	0.012
35	A35	110	2.89	2.9183	0.008
36	A36	112	2.94	2.9578	0.005
37	A37	117	3.07	3.0550	0.006
38	A38	125	3.28	3.2064	0.023
39	A39	130	3.41	3.4929	0.024

40	A40	135	3.55	3.5891	0.010
41	A41	142	3.73	3.7212	0.002
42	A42	129	-	3.4734	-
43	A43	131	-	3.5122	-
44	A44	133	-	3.5508	-
45	A45	142	-	3.7212	-
46	A46	147	-	3.8139	-
47	A47	157	-	3.9954	-
48	A48	163	-	4.1020	-
49	A49	150	-	3.8688	-
50	A50	160	-	4.0489	-

The extension and comparison of the data of the Rc in plant, which is obtained from the proposed mathematical model, with the experimental values of other references [12].

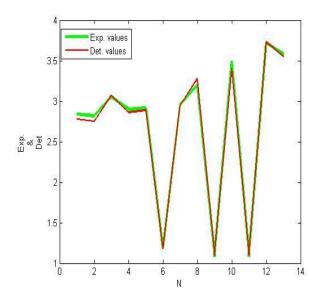


Fig.4 Errors between the values obtained by the proposed approximate mathematical model in table 2, and the experimental values [12].

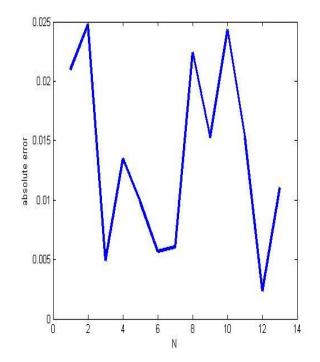


Fig.5 Errors between the values obtained by the proposed approximate mathematical model in table

2, and the experimental values [12].

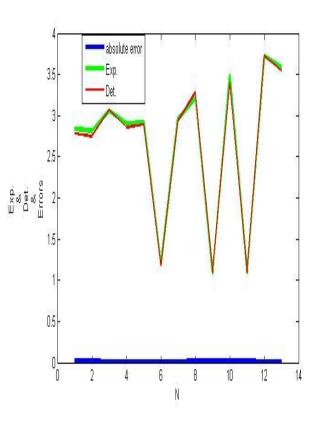
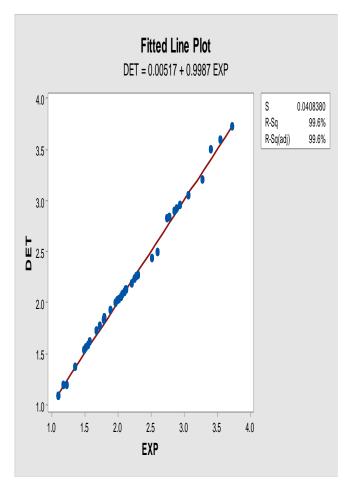


Fig.6 Comparison between proposed model and experimental values in [12], and errors.

5- Statistical analysis:

To make a more reliable model, a statistical analysis is conducted on the proposed model. We found out that R-Sq is 99.6 % where the range of R-Sq should not be less than 35%; this shows that the equation of the model is appropriate to desired aim of the study as shown in the following regression analysis:



LINEAR

Regression Analysis: DET versus EXP

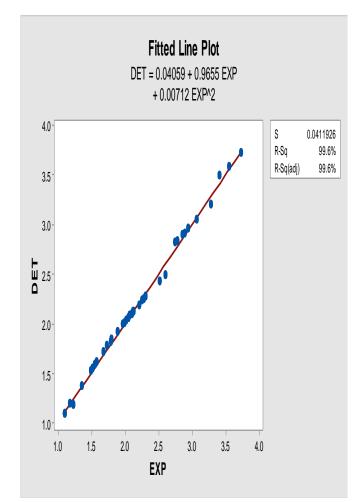
The regression equation is

DET = 0.00517 + 0.9987 EXP

S = 0.0408380 R-Sq = 99.6% R-Sq(adj) = 99.6%

Analysis of Variance

Source	DF	SS	MS	F	Р
Regression 0.000006	1	1′	7.9003	17.9003	10733.30
Error	39	0.0650	0.001	7	
Total	40	17.9654	4		



QUADRATIC

Polynomial Regression Analysis: DET versus EXP

The regression equation is

DET = 0.04059 + 0.9655 EXP + 0.00712 EXP^2

S = 0.0411926 R-Sq = 99.6% R-Sq(adj) = 99.6%

Analysis of Variance

P- ISSN 1991-8941 E-ISSN 2706-6703 2017,11 (1):56-67

Journal of University of Anbar for Pure Science (JUAPS)

Open Access

Source DF SS MS F P	$DET = -0.2406 + 1.382 EXP - 0.1835 EXP^2 +$
Regression 2 17.9009 8.95046 5274.82 0.00008	0.02718 EXP^3
Error 38 0.0645 0.00170	S = 0.0404362 R-Sq = 99.7% R-Sq(adj) = 99.6%
Total 40 17.9654	Analysis of Variance
	Source DF SS MS F P
Sequential Analysis of Variance	Regression 3 17.9049 5.96830 3650.14 0.00003
Source DF SS F P	Error 37 0.0605 0.00164
Linear 1 17.9003 10733.30 0.000006	Total 40 17.9654
Quadratic 1 0.0006 0.33 0.568	Sequential Analysis of Variance
Fitted Line Plot	
DET = - 0.2406 + 1.382 EXP	Source DF SS F P
- 0.1835 EXP^2 + 0.02718 EXP^3	Linear 1 17.9003 10733.30 0.000
R-Sq 99.7%	Quadratic 1 0.0006 0.33 0.568
3.5 - R-Sq(adj) 99.6%	Cubic 1 0.0040 2.43 0.127
3.0-	Orthogonal Regression Analysis: DET versus EXP
u 25-	Error Variance Ratio (DET/EXP): 0.05
20-	Regression Equation
and the second	DET = -0.002 + 1.002 EXP
1.5-	Coefficients
1.0 1.5 2.0 2.5 3.0 3.5 4.0	Predictor Coef SE Coef Z P
EXP	Approx 95% CI
CUBIC	Constant -0.00236 0.0220283 -0.1073 0.915 (-
	0.045538; 0.04081)
Polynomial Regression Analysis: DET versus EXP	EXP 1.00217 0.0096737 103.5974 0.000 (
The regression equation is	0.983210; 1.02113)

Error Variances

Variable Variance

DET 0.0000774

EXP 0.0015473

Finally, it is worth mentioning that the good mathematical models must have the following: of a number of variables; clear and precise definition of these variables; accurate measurement of these variables; and finding a mathematical relationship of some sort between these variables [14]. The current model is proved to have the above characteristics; this states that it is a suitable to achieve its aim of calculating the effects of radioactivity of Cs ¹³⁷ on the plant.

6- Mathematical formula by using Nevill's method:

By using Nevill's formula we get:

$$N_0 = 42$$
 , $R_{C0} = 1.1$

$$N_1 = 142$$
, $R_{c1} = 3.73$

 $=\frac{(N-42)3.73-(N-142)1.1}{142-42}$

$$R_{c} = \frac{(N - N_{0})R_{c1} - (N - N_{1})R_{c0}}{(N_{1} - N_{0})}$$
$$= \frac{3.73N - 156.66 - 1.1N + 156.2}{100}$$
$$- 2.63N - 0.46$$

 $R_c = 0.0263 N - 0.0046$

100

Comparison between the values, determined via the proposed Novell's formula, to determination the R_c in plant, and the experimental values of other references [12], as shown in the following table 3.

Table 3. Comparison between the values,
determined by the proposed Novell's formula, to
calculation the R _c in plant, and the experimental
volues [12]

	values [12].						
No.	Area (A)	N	Rc Exp. [12]	Rc Det.	%		
1	A ₁	117	3.07	3.072	0.00065		
2	A_2	109	2.86	2.862	0.0007		
3	A 3	110	2.89	2.888	0.000692		
4	A4	45	1.18	1.178	0.001695		
5	A 5	112	2.94	2.941	0.00034		
6	A 6	125	3.28	3.282	0.00061		
7	A 7	96	2.52	2.520	0.00000		
8	A 8	57	1.49	1.494	0.00268		
9	A9	86	2.26	2.257	0.001327		
10	A10	76	1.99	1.994	0.00201		
11	A ₁₁	59	1.55	1.547	0.001935		
12	A ₁₂	81	2.13	2.125	0.002347		
13	A ₁₃	72	1.89	1.889	0.000529		
14	A14	69	1.8	1.810	0.00556		
15	A15	80	2.1	2.099	0.000476		
16	A16	99	2.6	2.599	0.000385		
17	A17	106	2.78	2.783	0.00108		

P- ISSN 1991-8941 E-ISSN 2706-6703 2017,11 (1):56-67

18	A18	60	1.58	1.573	0.00443
19	A19	80	2.1	2.099	0.000476
20	A20	78	2.05	2.046	0.001951
21	A ₂₁	58	1.52	1.520	0.00000
22	A ₂₂	84	2.21	2.204	0.002715
23	A23	77	2.02	2.020	0.00000
24	A24	68	1.79	1.783	0.003911
25	A25	88	2.31	2.309	0.000433
26	A ₂₆	79	2.07	2.073	0.00145
27	A27	75	1.97	1.967	0.001523
28	A28	66	1.73	1.731	0.00058
29	A29	78	2.05	2.046	0.001951
30	A ₃₀	87	2.28	2.283	0.00132
31	A ₃₁	64	1.68	1.678	0.00119
32	A32	81	2.12	2.125	0.00236
33	A33	88	2.31	2.309	0.000433
34	A34	105	2.75	2.756	0.00218
35	A35	52	1.36	1.363	0.00221
36	A36	47	1.23	1.231	0.00081
37	A37	42	1.1	1.1	0.00000

38	A38	130	3.41	3.414	0.00117
39	A39	42	1.1	1.1	0.00000
40	A40	142	3.73	3.73	0.00000
41	A41	135	3.55	3.545	0.001408

Note: (A) refers to the samples of (41) areas.

By using Novell's formula, the relationship between the radioactive and the area has been found as linear equation. While in the approximate mathematical model, the equation is nonlinear, which is preferred in the application of the mathematical model because the radioactive is nonlinear phenomenon as well as the linear equation is considered weak in the application.

References

- [3] Fritzson, P. (2010). Principles of object-oriented modeling and simulation with Modelica 2.1. John Wiley & Sons.
- [4] Ritchie, J. C., & McHenry, J. R. (1990). Application of radioactive fallout cesium-137 for measuring soil erosion and sediment accumulation rates and patterns: a review. *Journal of environmental quality*, 19(2), 215-233.
- [5] Aris, R. (1999). Mathematical modeling: a chemical engineer's perspective (Vo. 1). Academic Press.
- [6] Weimerskirch, H., Le Corre, M., Jaquemet, S., Potier, M., & Marsac, F. (2004). Foraging strategy of a top predator in tropical waters: great frigatebirds in the Mozambique Channel. *Marine* ecology progress series, 275, 297-308.

- [8] Little, Todd. D. (2013). *Longitudinal structural equation modeling*. Guilford Press.
- [9] Arif, G. E., Al-Douri, Y. "Mathematical Modeling of Physical Properties for Hexagonal Binaries". Scholar's Press, Germany. 2016.
- [10] Abu-Farsakh, H., & Qteish, A. (2007). Ionicity scale based on the centers of maximally localized Wannier functions. *Physical Review B*, 75(8), 085201-085206.
- [11] Arif, G. E., Abdullah, F. A., & Al-Douri, Y. (2014). Modeling of the Electronic Properties of Hexagonal Semiconductors. *Advanced Materials Research Vo. 925*, pp. 364-368.
- [12] Rasheed M. Yousef, Hana I. Hassan & Ahmad Kh. Emhemed. (2008) 'Determination of the specific activity of Cs¹³⁷ and K⁴⁰ in environment Nineveh governorate' *Journal of Al-Rafedain Sciences*, Vo. 19 (2), 205-220.

- [13] Gene H. Golub; Charles F. Van Loan (1996). *Matrix Computations – Third Edition*. The Johns Hopkins Studies in the Mathematical Sciences University Press, Baltimore and London. P. 53. ISBN 0-8018-5413-X.
- [14] Flash, T., & Hogan, N. (1985). The coordination of arm movements: an experimentally confirmed mathematical model. *Journal of neuroscience*, 5(7), 1688-1703.
- [15] لحمر، صالح، (2007). فاعلية برنامج مقترح في تنمية مهارات النمذجة الرياضية لدى الطلاب المعلمين شعبة الرياضيات بكلية التربية جامعة عدن رسالة ماجستير، كلية التربية، جامعة عدن، عمان.
- [16] أبو عميرة، محبات، (2000). تعليم الرياضيات بين النظرية والتطبيق. الطبعة الثالثة القاهرة: الدار العربية للكتاب.
- [17] السعيد، رضا، (1989). نموذج منظومي رياضي متعدد الأبعاد لاشتقاق مجالات البحوث الأكاديمية في تعليم وتعلم الرياضيات في كليات التربية. مجلة كلية التربية، جامعة المنوفية، الجزء الثاني، العدد(4).

القتراح نموذج رياضي تقريبي لحساب التأثير الإشعاعي للسيزيوم على النبات
خسان عزالدين عارف.

الخلاصة:

تهدف هذه الدراسة إلى حساب نظري للتأثير الأشعاعي للسيزيوم ¹³⁷ Cs على النبات في محافظة نينوى عن طريق اختيار 50 موقع كعينات من الدراسة. يتم إجراء الحسابات من خلال بناء نموذج رياضي يحدد نظريا التأثير الأشعاعي للسيزيوم ¹³⁷ Cs في النبات. في هذا البحث، تم ذكر الملامح الرئيسية وعملية النمذجة الرياضية واستخدامها بشكل واضح في عملية بناء النموذج الرياضي الذي يقوم بتحديد القيم المحسوبة للتأثير الأشعاعي للسيزيوم Cs¹³⁷ في النبات. القيم التي حسبت بالموديل المقترح تراوحت بين 1.1814 في (A₂₈) و A28 في (A₁₀). تمت مقارنة النتائج التي تم الحصول عليها من النموذج المبني مع قيم المراجع الأخرى. وظهرت نتيجة هذه المقارنة اتفاقا جيدا مع الدراسات الأخرى.